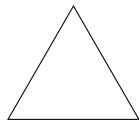
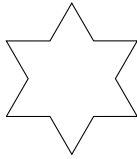


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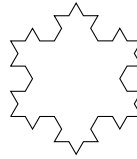
1. [10.2.96a] **Helga von Koch's snowflake curve.** Helga von Koch's snowflake is a curve of infinite length that encloses a region of finite area. To see why this is so, suppose the curve is generated by starting with an equilateral triangle whose sides have length 1.



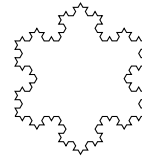
$C_1$



$C_2$



$C_3$



$C_4$

Find the length  $L_n$  of the  $n$ th curve  $C_n$  and show that  $\lim_{n \rightarrow \infty} L_n = \infty$ .

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2. [10.3.62] Consider the sequence  $\{1/n\}_{n=1}^{\infty}$ . On each subinterval  $(1/(n+1), 1/n)$  within the interval  $[0, 1]$ , erect the trapezoid with area  $a_n$  having heights  $y = 1/(n+1)$  at  $x = 1/(n+1)$  and  $y = 1/n$  at  $x = 1/n$ . Find the total area  $\sum a_n$  of all the rectangles.

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3. [10.9.43] Use the identity  $\sin^2 x = (1 - \cos 2x)/2$  to obtain the Maclaurin series for  $\sin^2 x$ . Then differentiate this series to obtain the Maclaurin series for  $2 \sin x \cos x$ . Check that this is the series for  $\sin 2x$ .

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4. [10.10.60b] Find the first three terms of the Taylor series for

$$\sinh^{-1} x = \int_0^x \frac{dt}{\sqrt{1+t^2}}$$

to estimate  $\sinh^{-1} 0.25$ . Give an upper bound for the magnitude of the estimation error.

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5. [10.Adv.31b] **Quality Control** In one throw of two dice, the probability of getting a roll of sum 7 is  $p = 1/6$ . If you throw the dice repeatedly, the probability that a 7 will appear for the first time at the  $n$ th throw is  $q^{n-1}p$ , where  $q = 1 - p = 5/6$ . The expected number of throws until a 7 first appears is  $\sum_{n=1}^{\infty} nq^{n-1}p$ . Find the sum of this series.